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**Lecture Notes on Economic Growth (II):
Five Prototype Models of Endogenous
Growth***

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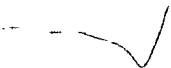
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